

the inputs to both amplifiers. Because  $|\bar{v}_0^2|$  and  $|\bar{v}_2^2|$  are functions of the equivalent noise resistance of the amplifiers,  $R_n$ , it is desirable to make  $R_n$  as small as possible.  $R_n$  for each amplifier was approximately 770 ohms at 300° K over a band width of 3 to 7 kc/s. This was derived by measuring the recorder deflection (or the squared r.m.s. voltage at the inputs to the multiplier) for  $|\bar{v}_0^2|$  and  $|\bar{v}_2^2|$  for various input resistances to the amplifiers at room temperature. For a band width of 3 to 12 kc/s the equivalent noise resistance of the amplifiers was 650 ohms. If one assumes that the flicker noise is proportional to  $1/f$ , then the equivalent noise resistance of the amplifiers at high frequencies is approximately 340 ohms. Therefore, flicker noise was the main contribution to  $R_n$  between 3 and 7 kc/s.

#### 4. Errors Due to Mismatch of the Time Constants in the $\pi$ Network

Equations (4) and (5) were derived under the condition that  $(\omega\tau_i)^2 \ll 1$  or that all the  $\tau$ 's are equal. If this does not hold, then equation (4) for  $T_0 = T_2$  is modified and one gets:

$$(4a) \quad \frac{T_0(R_0+R_2)}{T_1-2T_0} = R_1 \frac{1+(\omega^2\tau_0\tau_2)/(T_1-2T_0)\{T_1-T_0\tau_1[(1/\tau_0)+(1/\tau_2)]\}}{1+(\omega\tau_1)^2}$$

If

$$T_1 \gg T_0 \quad \text{and} \quad T_1 \gg T_0\tau_1\left(\frac{1}{\tau_0} + \frac{1}{\tau_2}\right),$$

one obtains:

$$(4b) \quad \frac{T_0(R_0+R_2)}{T_1-2T_0} \simeq R_1 \frac{1+(\omega\tau_1)^2(\tau_0\tau_2/\tau_1^2)}{1+(\omega\tau_1)^2} = R_1 f(\omega, \tau_1).$$

At helium temperatures it is then sufficient to make  $\tau_0\tau_2 \simeq \tau_1^2$ . The deviation of  $f(\omega, \tau_1)$  from unity will increase with increasing frequency. If both  $\tau_0$  and  $\tau_2$  are 10% larger than  $\tau_1$ , then the error at the upper half power frequency is less than 1%. The average error is smaller, because for lower frequencies the error decreases and  $\tau_1$  was always adjusted between  $\tau_0$  and  $\tau_2$ . For a systematic error in adjusting  $\tau_1$  the fractional error in the noise temperature is almost a constant in the liquid helium range.

#### 5. A-c. Resistance of Thermometer Elements

The deviation of the resistance of  $R_0$ ,  $R_1$ , and  $R_2$  in the audio-frequency range from their d-c. value was estimated to be approximately 0.1% (see above).

#### 6. Response of the Integrator

In the case of a narrow square noise band of width  $B$  and uniform spectral intensity a RC integrator of integration time  $\tau$  will measure with a relative error of a single measurement,  $\beta$ , (Burgess 1951):

$$(8) \quad \beta = \frac{[(A-\bar{A})^2]^{\frac{1}{2}}}{\bar{A}} = (2B\tau)^{-\frac{1}{2}},$$

where  $\bar{A}$  is the deflection of the recorder due to the d-c. component of the signal and  $(A-\bar{A})^2$  the mean-square deviation of the recorder due to the signal.